

Eddy covariance at Otway: A tale of two analysers



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Australian Government
Bureau of Meteorology

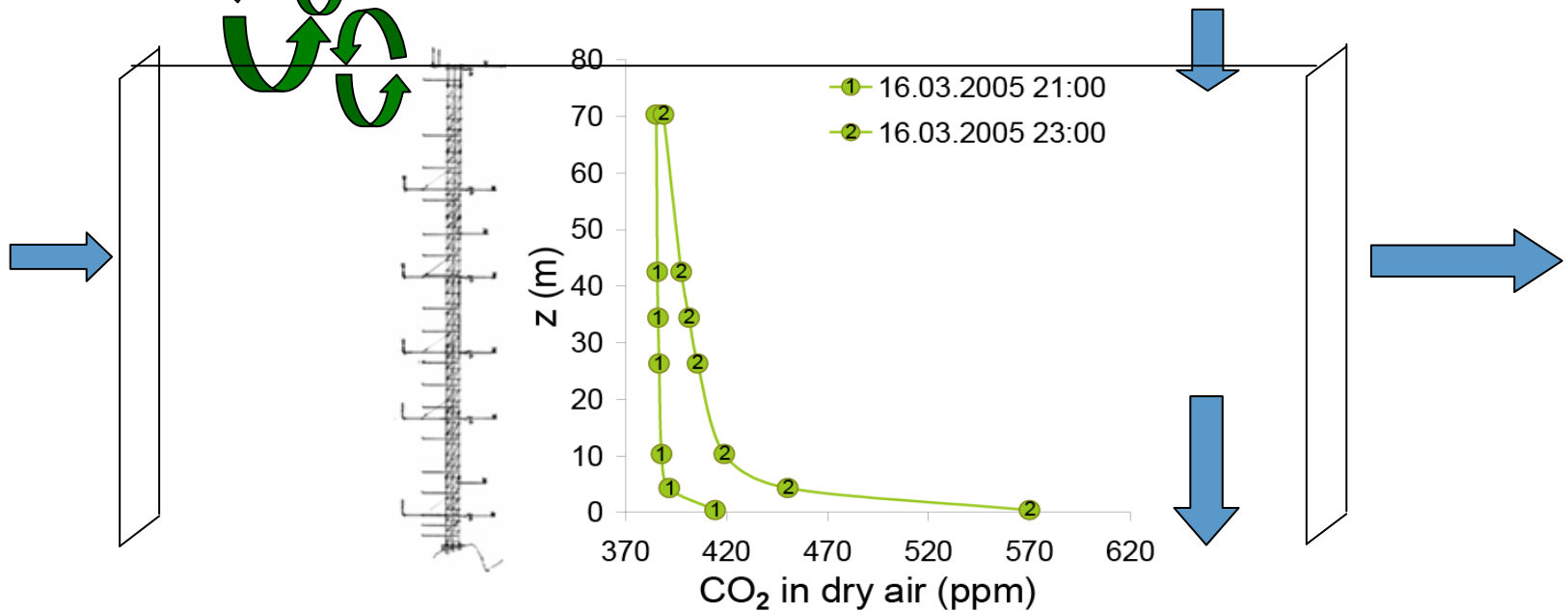
The Centre for Australian Weather and Climate Research
A partnership between CSIRO and the Bureau of Meteorology



With these assumptions

- Horizontally homogeneous flow

$$F_c = \overline{c_d} \overline{w' \chi_c'} + \int_0^h \overline{c_d} \frac{\partial \overline{\chi_c}}{\partial t} dz + \frac{1}{L^2} \int_0^L \int_0^L \int_0^h \left[\overline{u c_d} \frac{\partial \overline{\chi_c}}{\partial x} + \overline{v c_d} \frac{\partial \overline{\chi_c}}{\partial y} + \overline{w c_d} \frac{\partial \overline{\chi_c}}{\partial z} \right] dx dy dz$$



Eddy fluxes: Sonic anemometer gives

$$\overline{u}, \overline{v}, \overline{w} \quad \overline{u'}, v', w'$$

$$H = \rho \overline{c_{pd}} \overline{w' T'_v}$$

Where sonic virtual temperature is

$$T_v = T(1 + 0.514q)$$

Require H₂O & CO₂

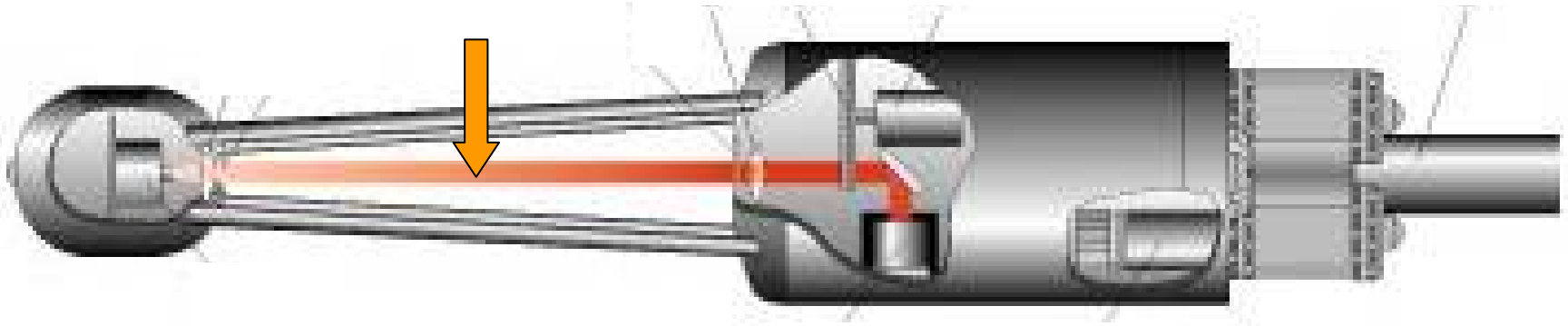
$$\lambda E = \lambda \overline{c_d} \overline{w' \chi'_v}$$

$$F_c = \overline{c_d} \overline{w' \chi'_c}$$

Note correlation of
vertical velocity
and mixing ratios

LI-7500 CO₂ and water vapour analyser

Measures mol m⁻³ in optical path,
not required mixing ratios χ_v χ_c



Eddy fluxes have been expressed
in terms of mixing ratio.

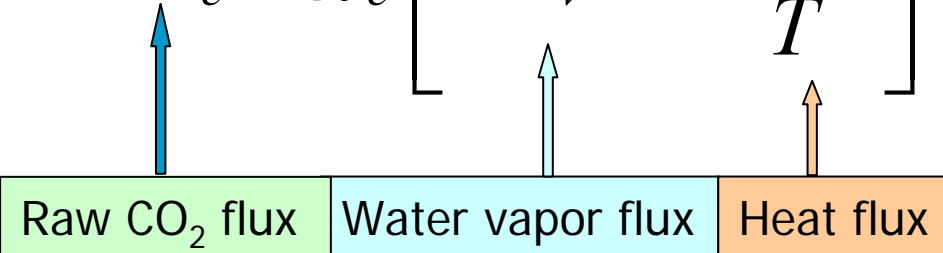
$$\overline{F_c} = \overline{c_d} \overline{w' \chi_c'}$$

What to do?

Eddy flux for trace gas - WPL theory (1980)

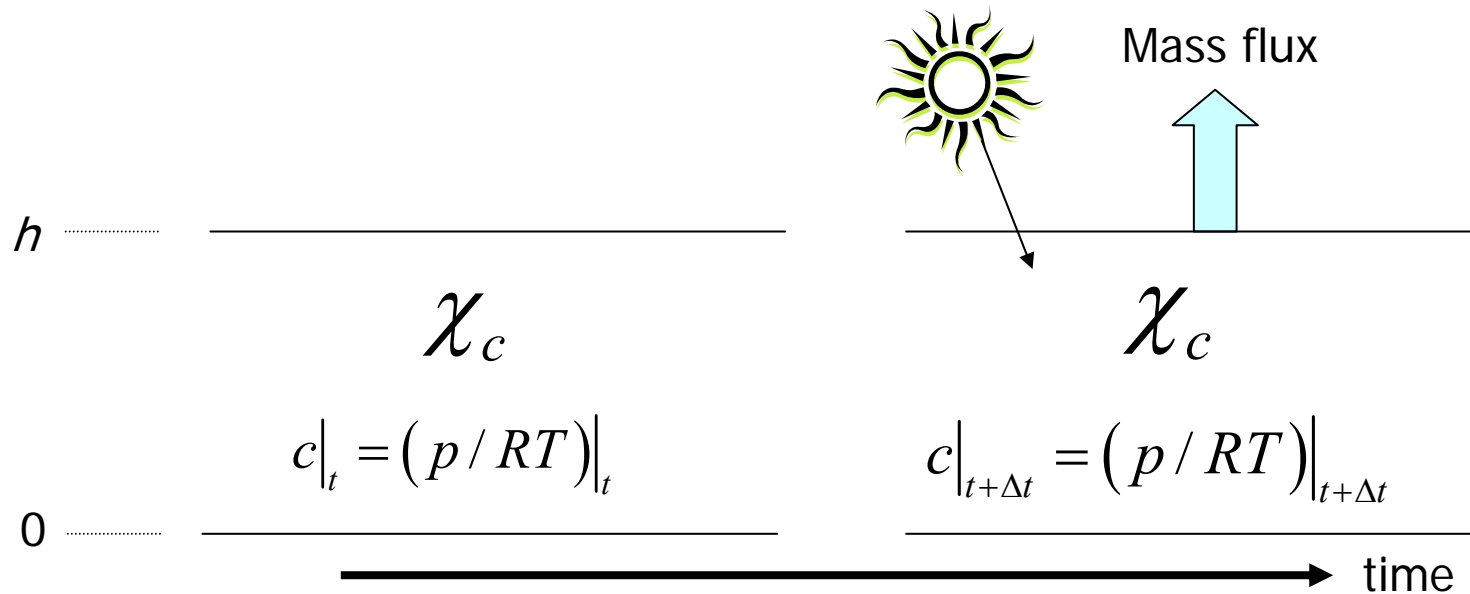
Steady state, horizontally homogeneous flow

- Open-path instruments

$$\overline{F_c} = \overline{c_d} \overline{w' \chi'_c} = \overline{w' c'_c} + \chi_c \left[\overline{w' c'_v} + \overline{c} \frac{\overline{w' T'}}{\overline{T}} \right]$$


The diagram illustrates the decomposition of the raw CO₂ flux into its constituent parts. At the bottom, there are three colored boxes: a green box labeled "Raw CO₂ flux", a light blue box labeled "Water vapor flux", and an orange box labeled "Heat flux". Three vertical arrows point upwards from these boxes to the equation above. A blue arrow points from the "Raw CO₂ flux" box to the term $\overline{w' c'_c}$. A light blue arrow points from the "Water vapor flux" box to the term $\overline{w' c'_v}$. An orange arrow points from the "Heat flux" box to the term $\overline{w' T'}$ within the bracketed expression.

What about non-steady state, horizontally homogeneous flow?



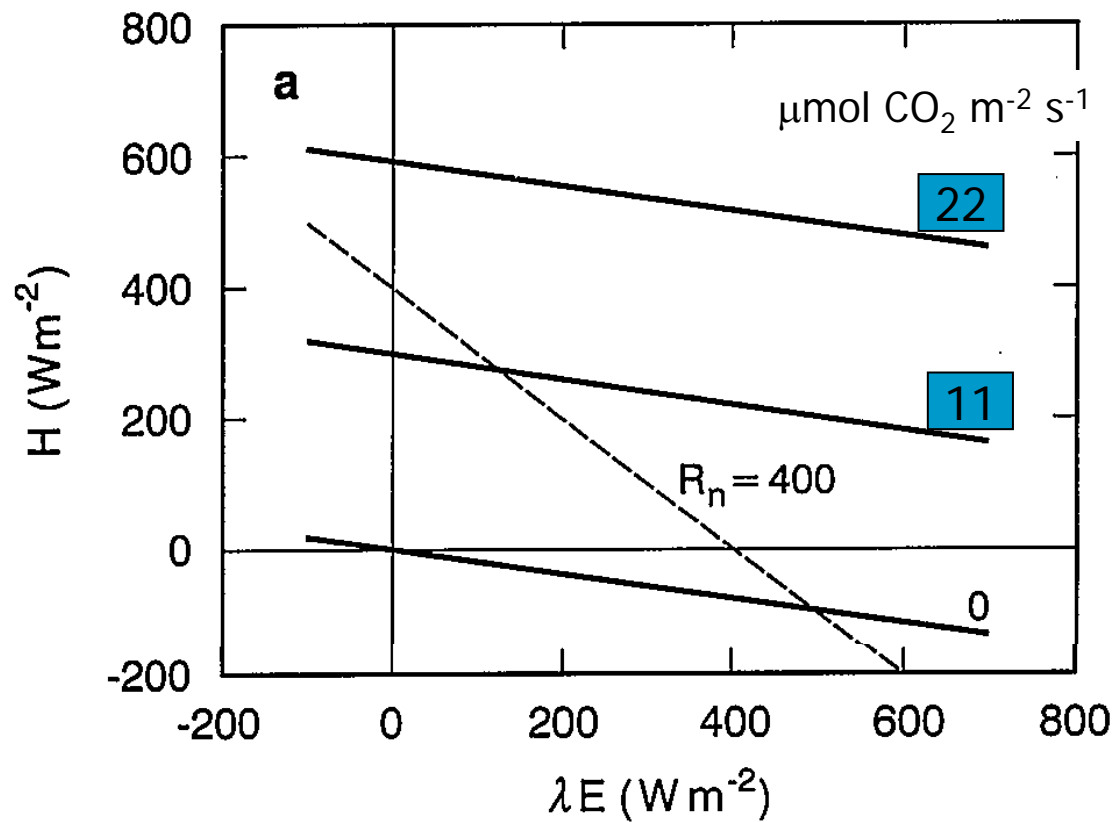
Change in concentration, but **not** mixing ratio

Leuning (2007) showed original WPL still OK

$$\overline{F_c} = \bar{c}_d \overline{w' \chi'_c} = \overline{w' c'_c} + \chi_c \left[\overline{w' c'_v} + \bar{c} \frac{\overline{w' T'}}{\bar{T}} \right]$$

Magnitude of WPL corrections for CO₂



– add to raw flux



Frequency domain - Covariance

Covariance
= eddy flux

$$\overline{w' \chi_c'} \equiv \frac{1}{\Delta t} \int_t^{t+\Delta t} w' \chi_c' dt \approx \int_0^\infty C_{w\chi_c}(n) dn$$

 Time domain  Frequency domain

$C_{w\chi_c}$ = contribution of total covariance of $w\chi_c$ per unit dn

Approximation because calculations are over a finite time interval Δt

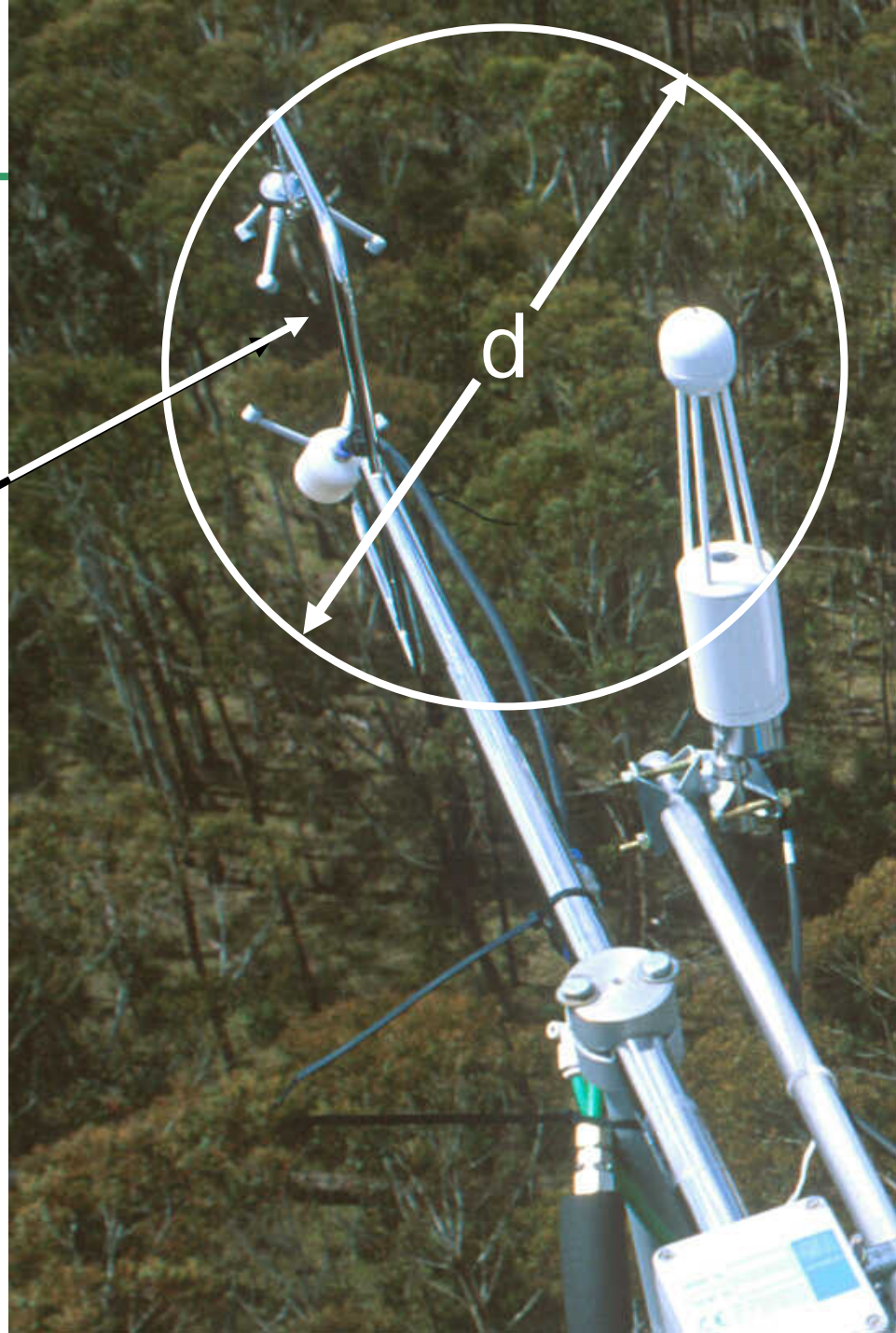
Instrument array is a low-pass frequency filter

Line-averaging along instrument path

- loss of variance

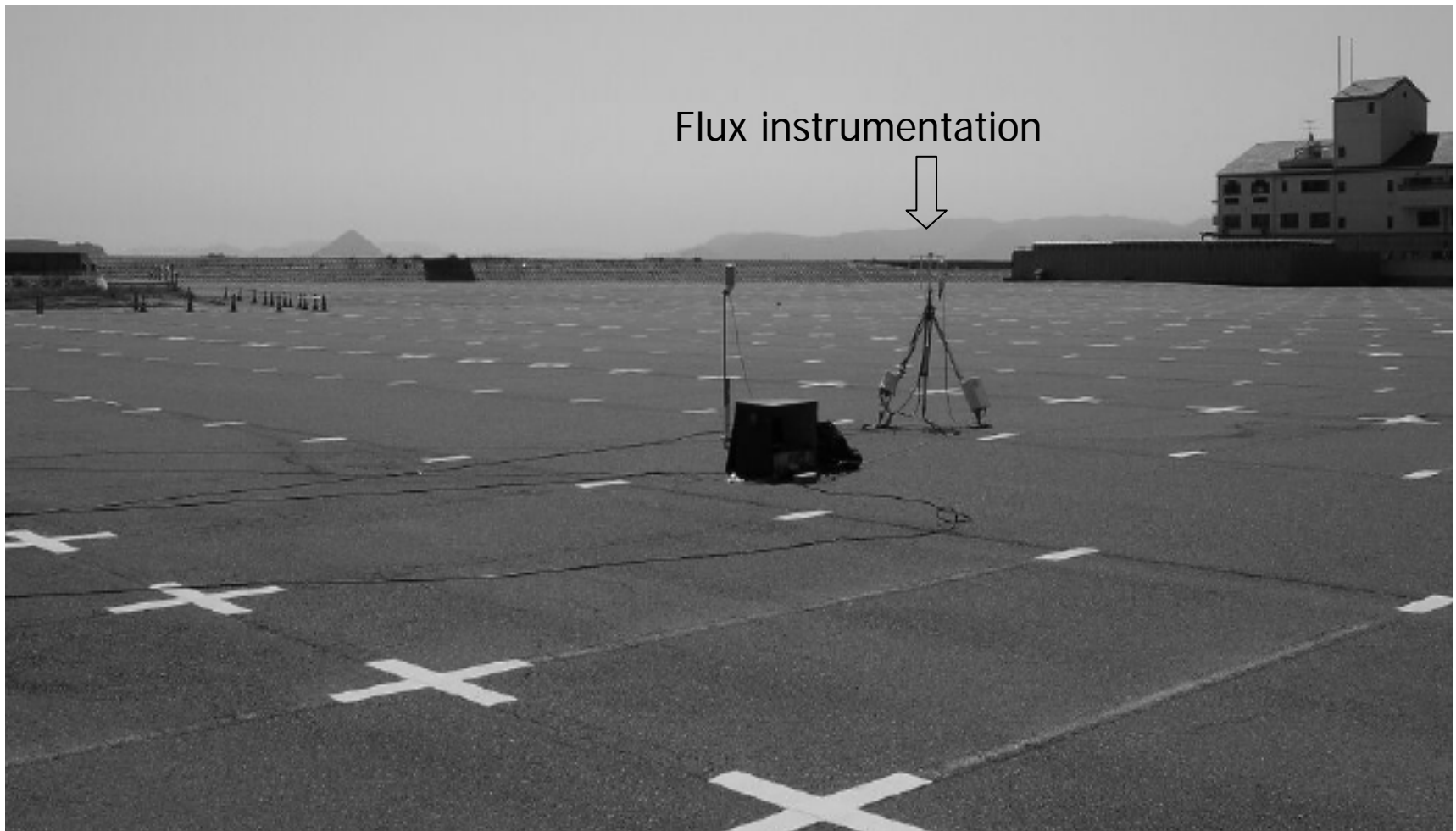
Spatial separation between instruments

- loss of covariance
- Samples eddies $> \sim 2d$



A case study – zero CO₂ flux over a car park

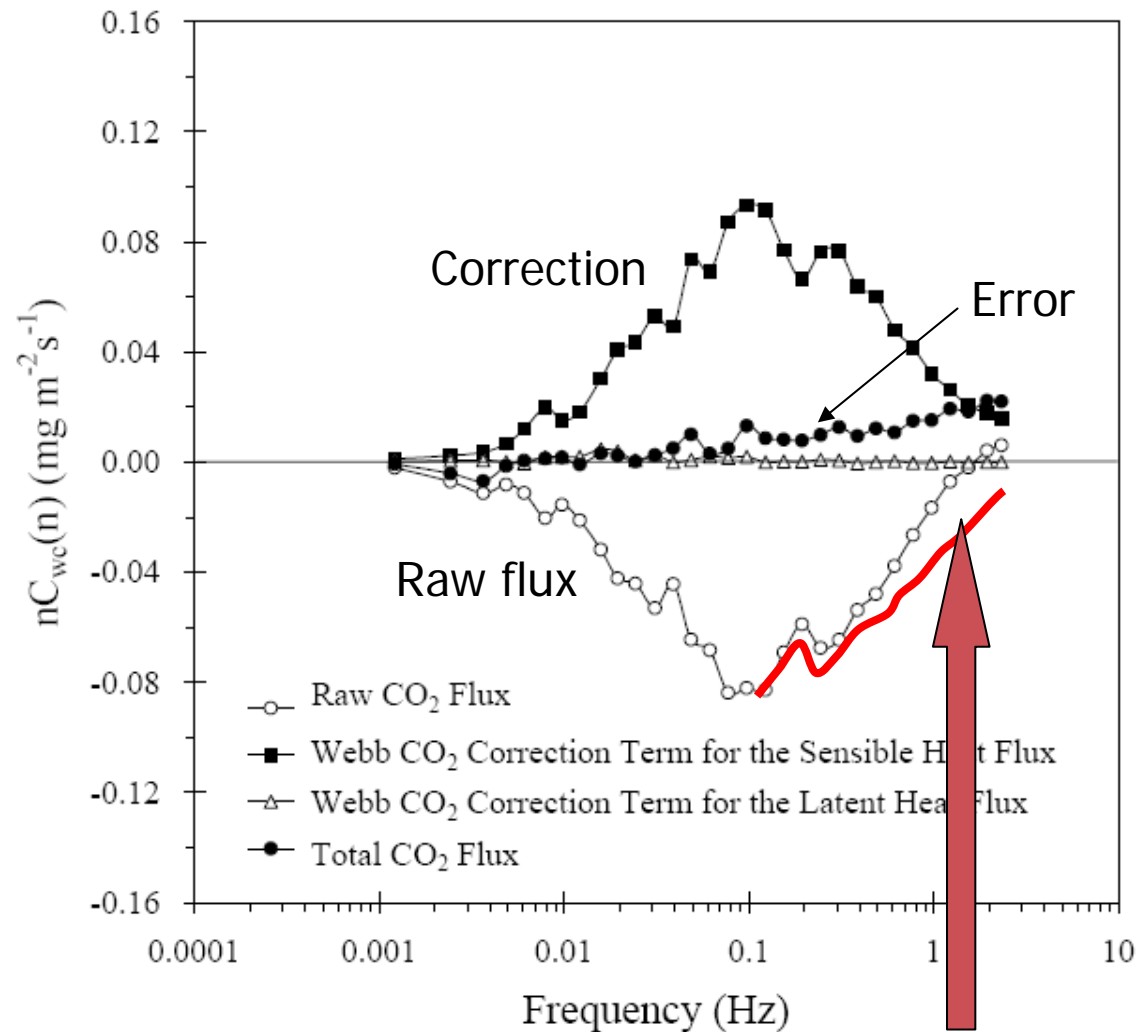
Kondo and Tsukamoto (2008)



WPL correction

Correction may be larger than true flux

Measurements of heat and water vapor fluxes must be accurate and have same frequency response as open-path CO_2 system



Need to correct for loss of covariance before WPL correction

Frequency Response Corrections

Define correction factor

$$C_F = \frac{\int_0^{\infty} C_{wc}(f) df}{\int_0^{\infty} G_{wc}(f) C_{wc}(f) df}$$

← 'true' cospectrum, eg $w'T'$

← filtered cospectrum

↑
filter function

$C_F > 1$, typically

(Leuning and Moncrieff, 1990; Leuning & Judd 1996)

Open path measurements – calculation sequence

$$1) \quad \overline{H} = \overline{\rho c_p} \overline{w' T'}$$

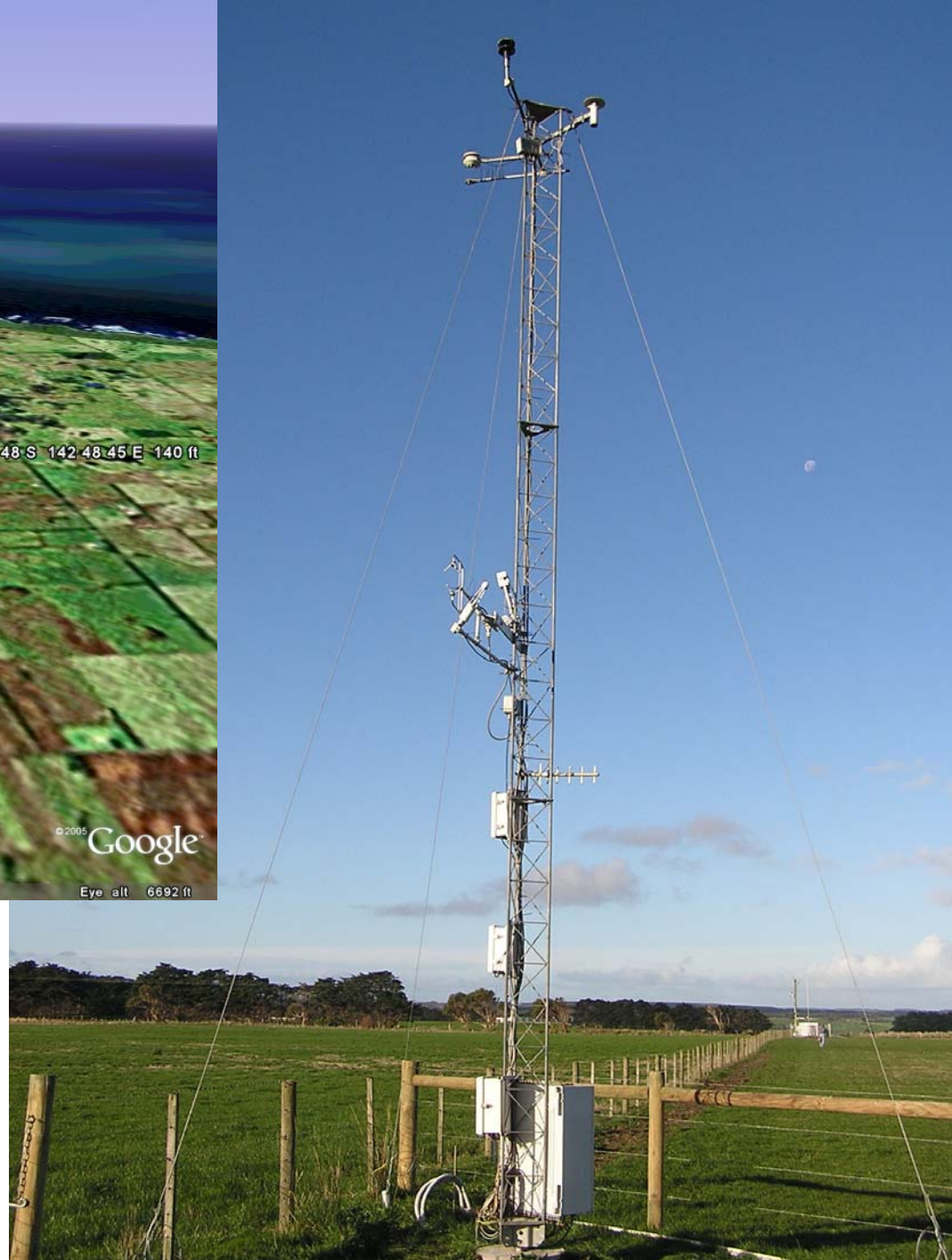
$$2) \quad \overline{E} = (1 + \overline{\chi_v}) \left[\overline{w' c'_v} + \frac{\overline{c_v}}{\overline{T}} \frac{\overline{H}}{\overline{\rho c_p}} \right]$$

$$3) \quad \overline{F_c} = \overline{w' c'_c} + \overline{c_c} \left[\frac{\overline{E}}{\overline{c}} + \frac{\overline{H}}{\overline{\rho c_p T}} \right]$$

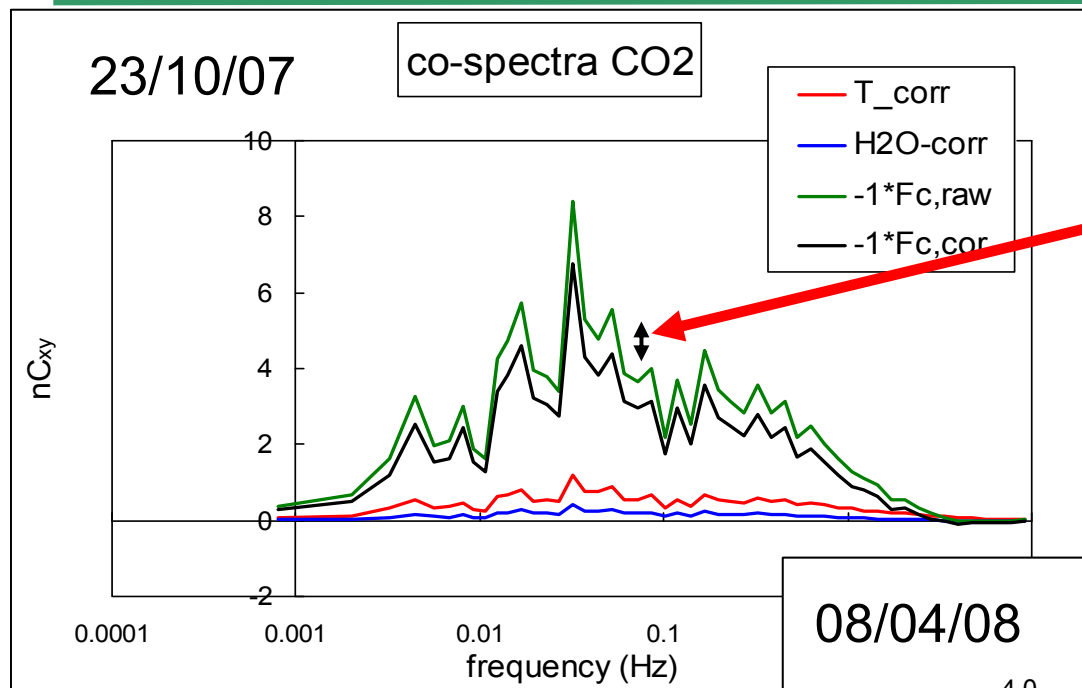
Assumes H , E & F_c have already been corrected for high & low frequency filtering



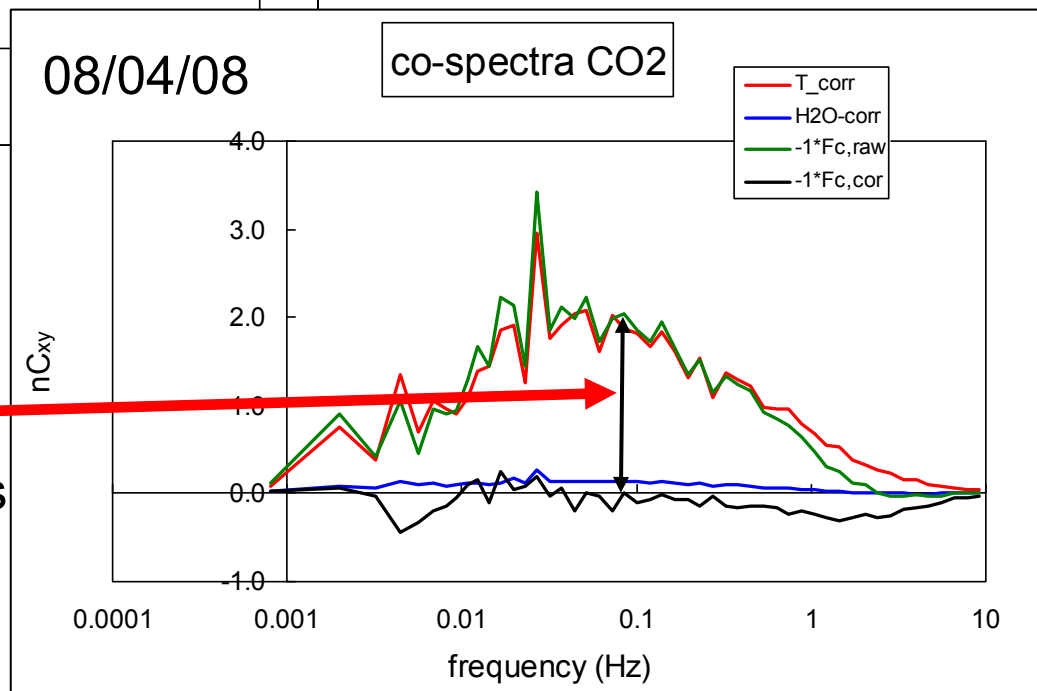
Otway flux station



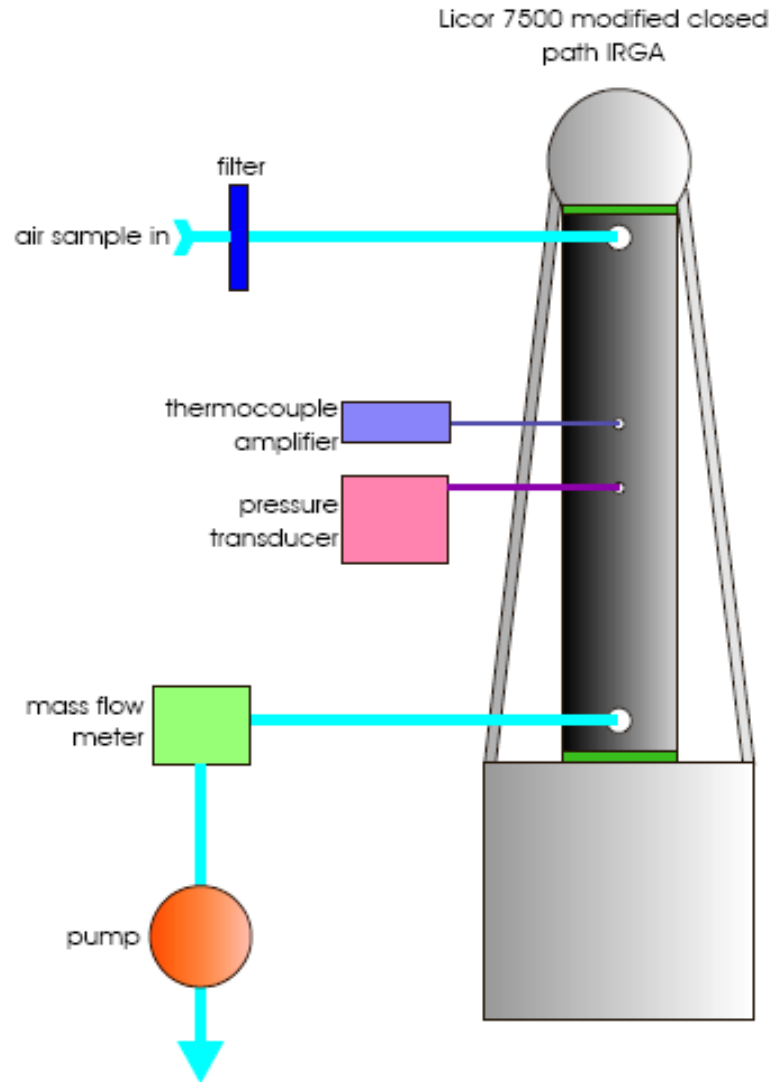
WPL corrections to open path measurements



Big wT, wq
WPL corrections



Conversion of LI7500 to closed-path analyser



Modified LI7500



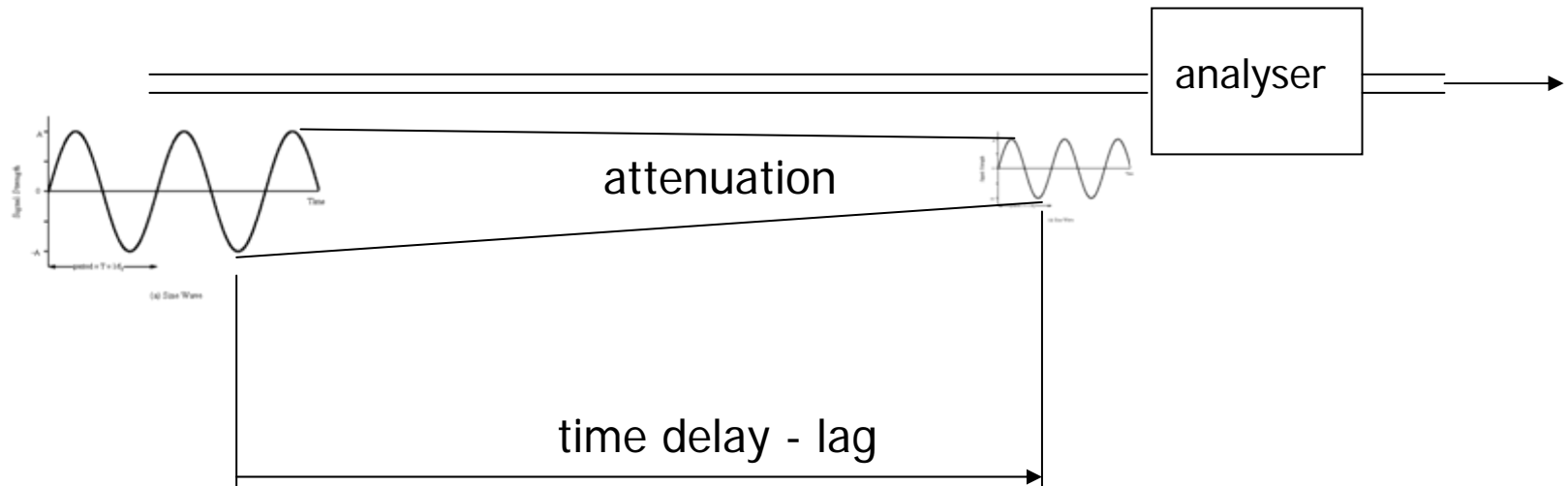
Closed-path analyser

- Measure c_c , c_v , T & P simultaneously in gas analyser and calculate mixing ratio at sampling rate used for eddy covariance

$$\chi_v = \frac{c_v}{P_i / (RT_i) - c_v}, \quad \chi_c = \frac{c_c}{P_i / (RT_i) - c_v}$$

- Must also consider
 - Time-lag
 - Hi-frequency attenuation by air flow in tubing

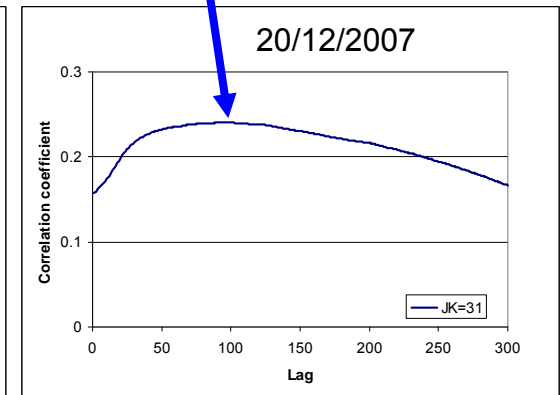
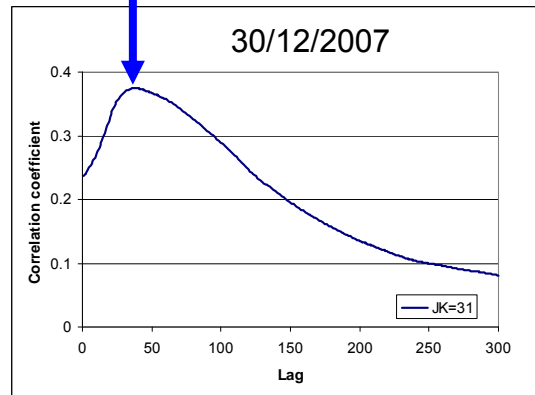
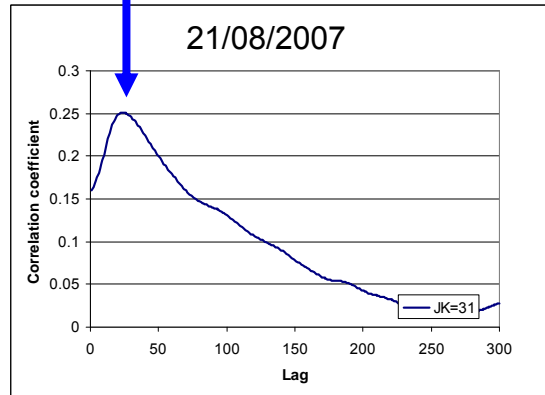
Closed-path gas sampling



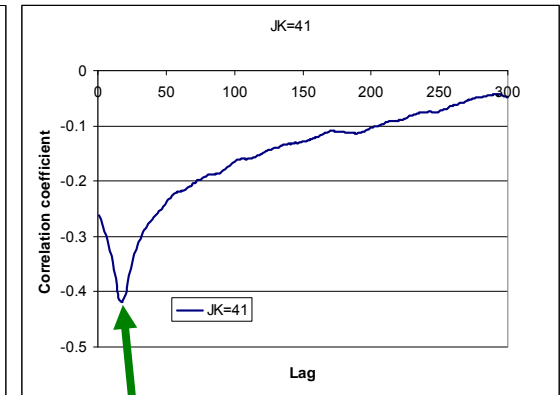
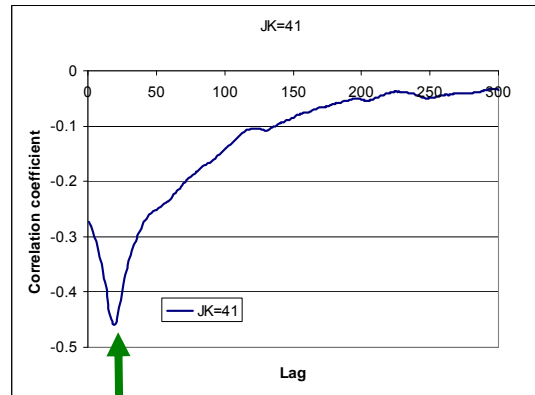
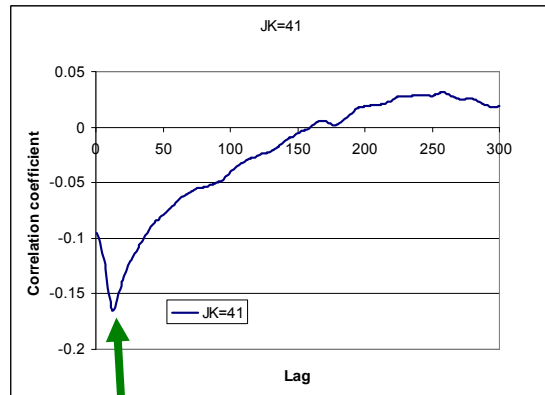
Lag at maximum correlation for closed path

H₂O lag @ max. correlation function of flow rate & rel. humidity

H₂O



CO₂



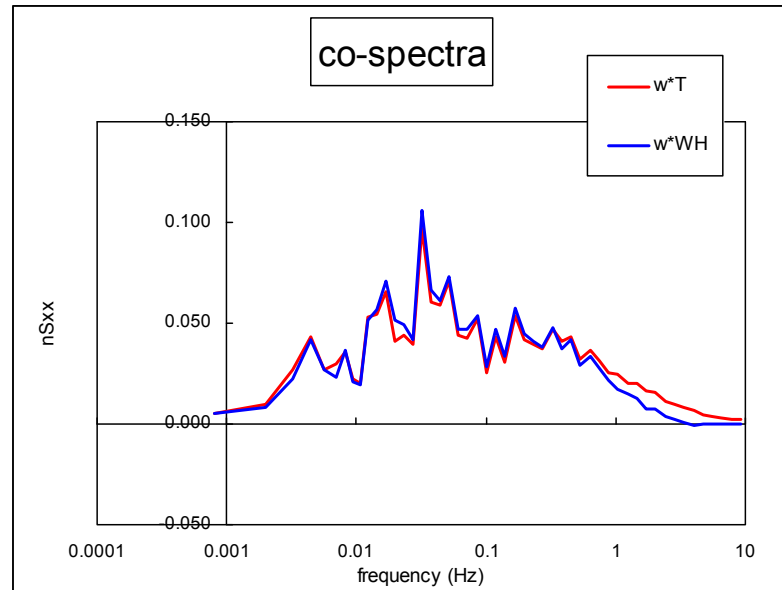
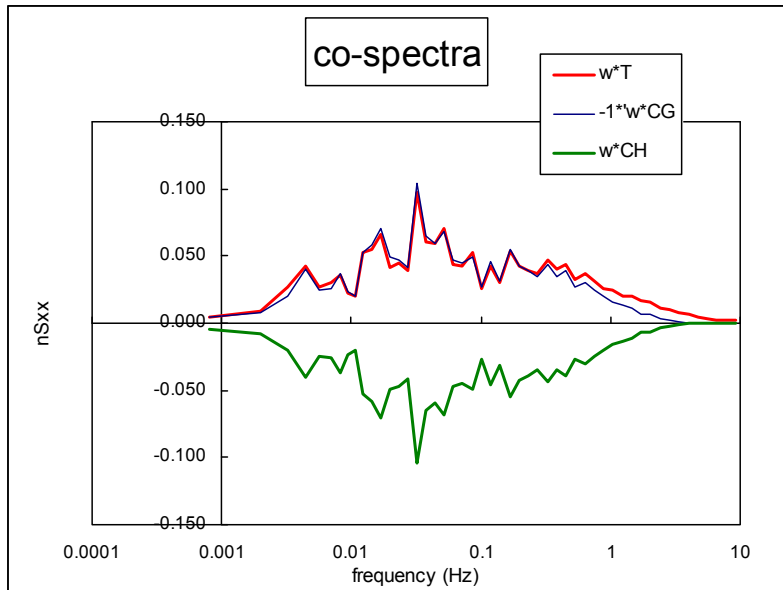
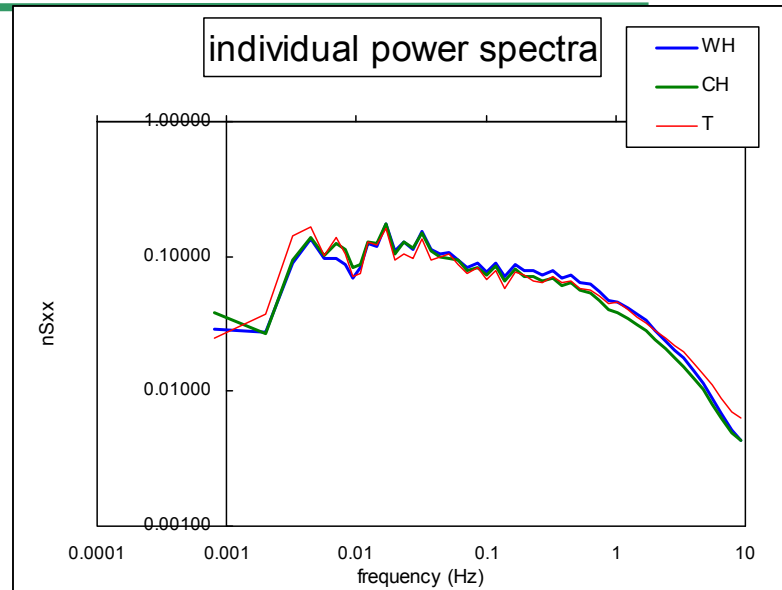
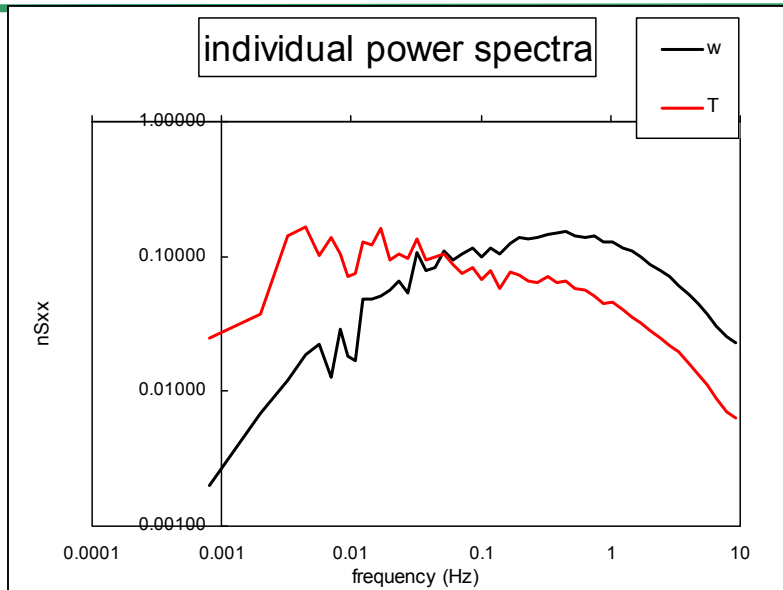
CO₂ lag @ max. correlation function of flow rate only

High Frequency Attenuation - Closed path

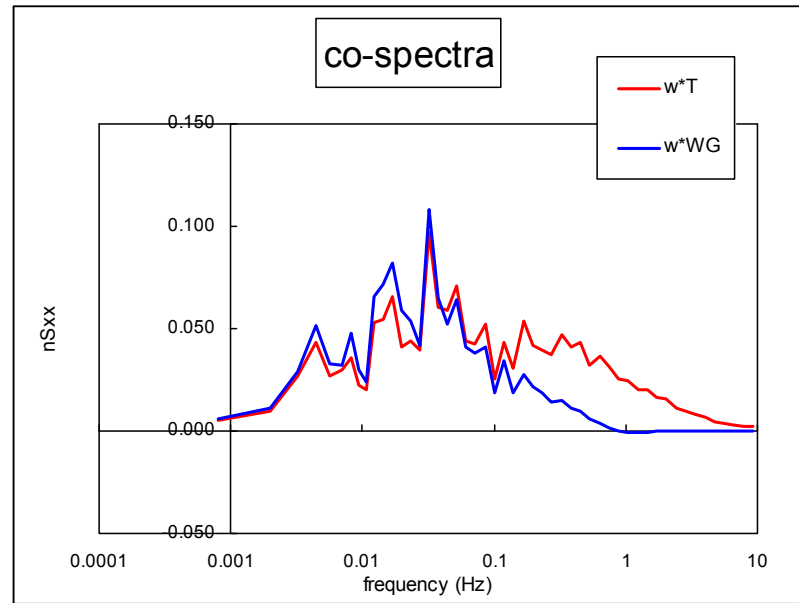
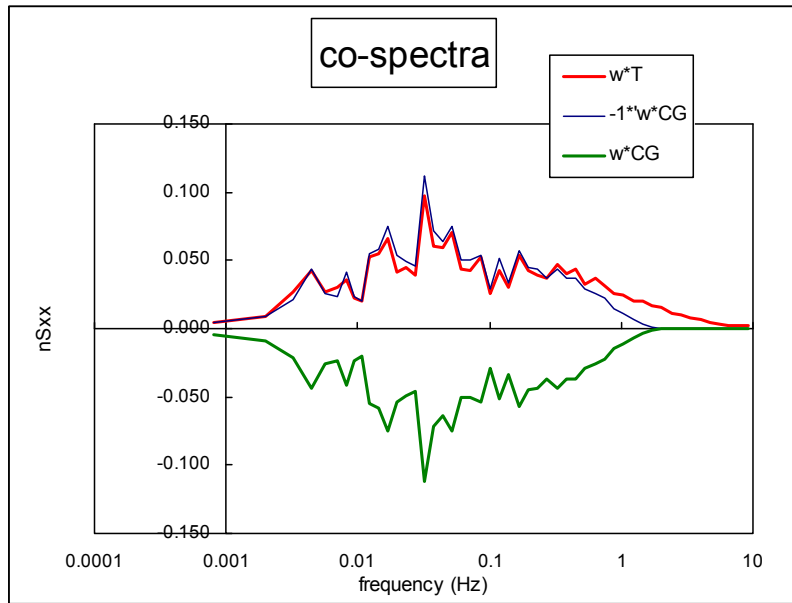
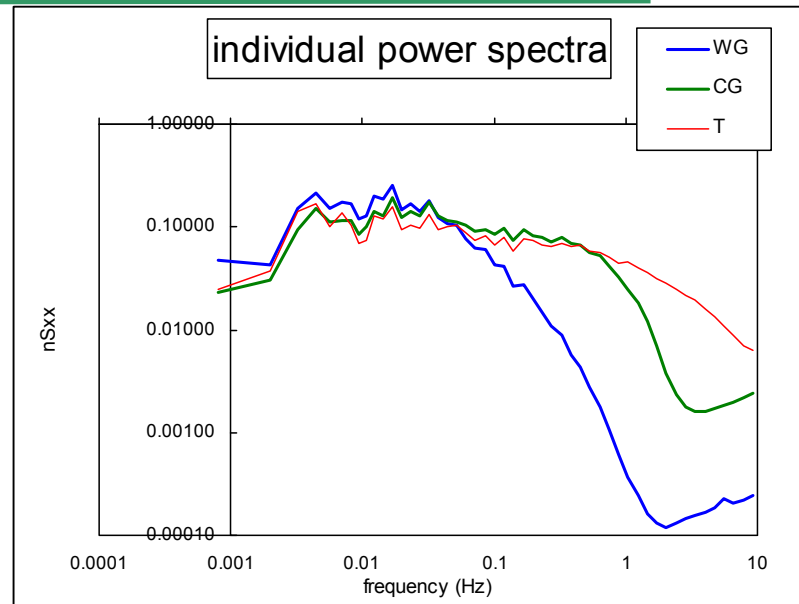
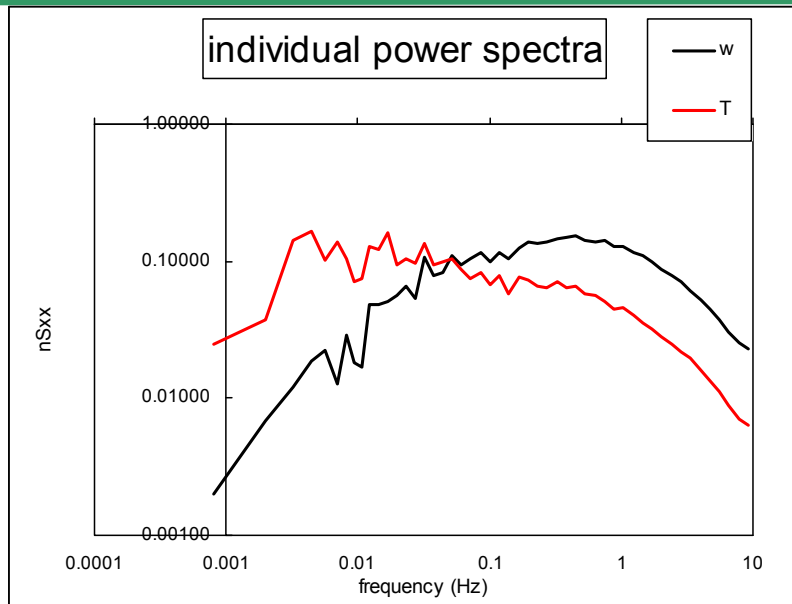
- Tubing acts like a low-pass filter by mixing the air
- Higher frequencies strongly attenuated – depends on:
 - Flow rate through tube
 - Tube diameter, length and material
 - Adsorption/desorption of gases on filter tubing walls

(Leuning and Moncrieff, 1990; Leuning & Judd 1996)

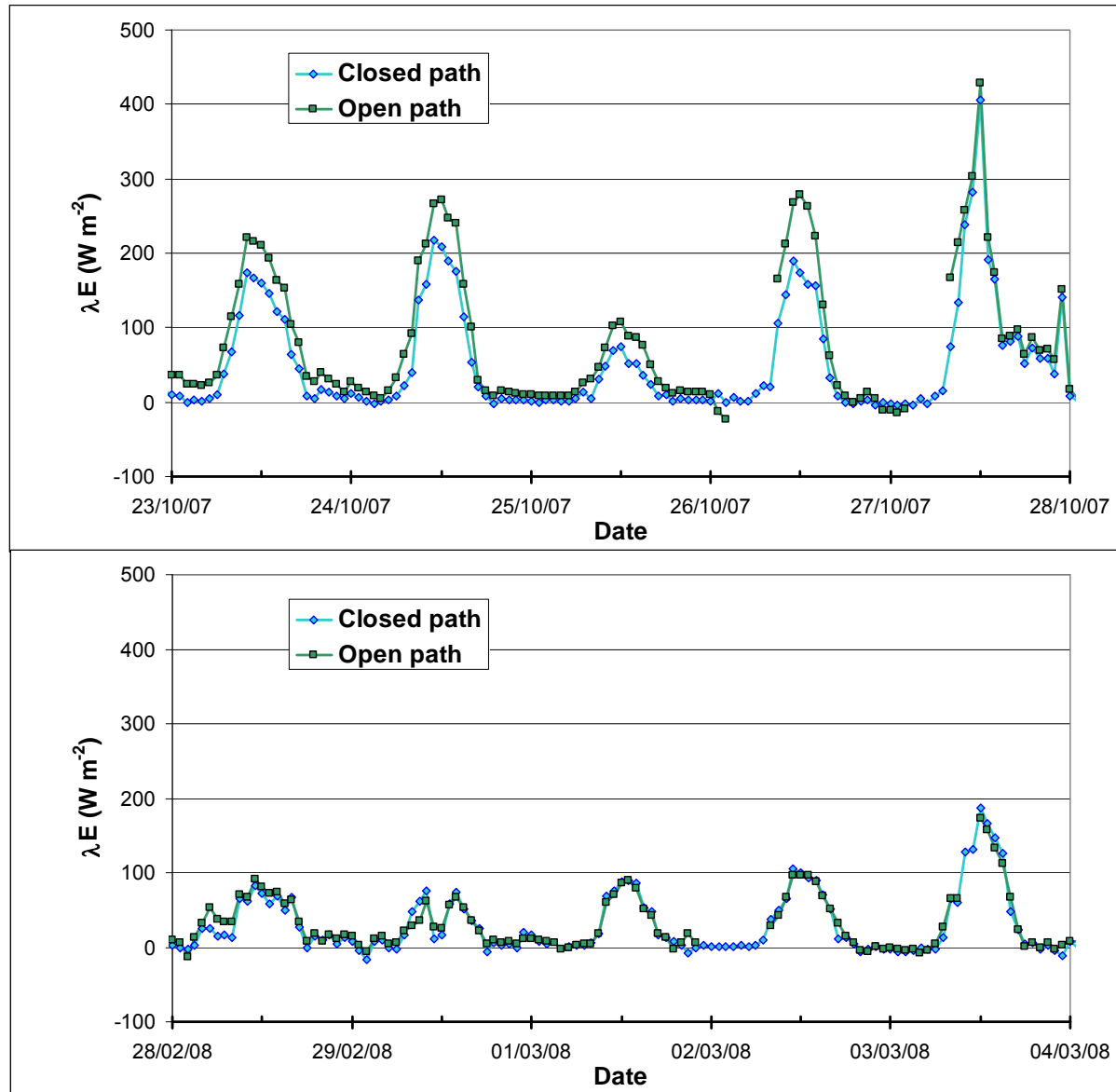
Open path spectra and co-spectra



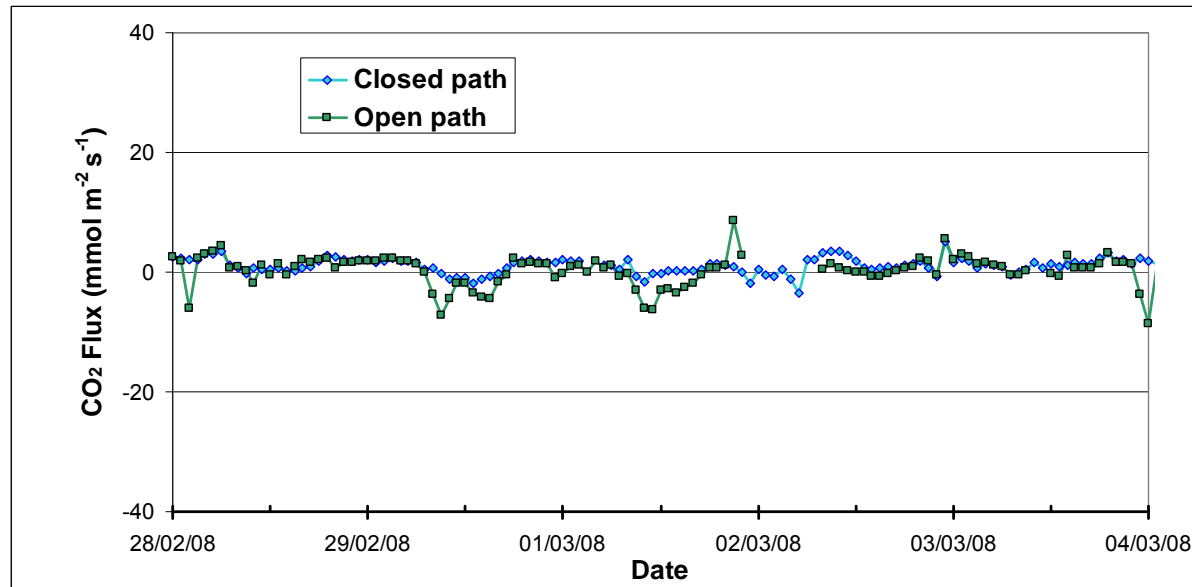
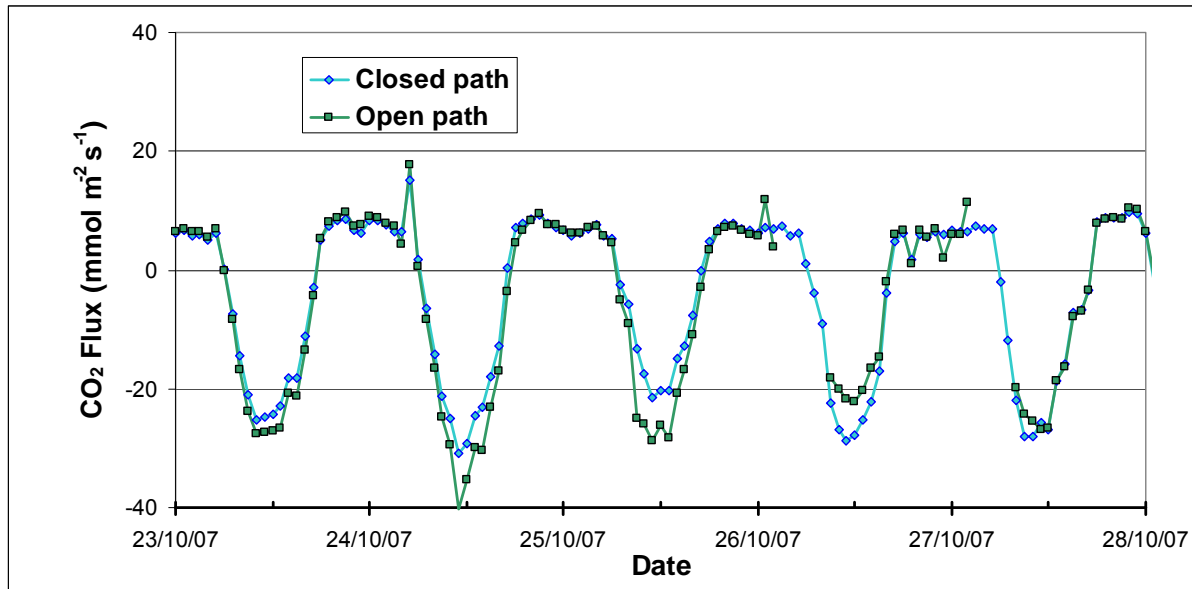
Closed path spectra and co-spectra



Time series of λE

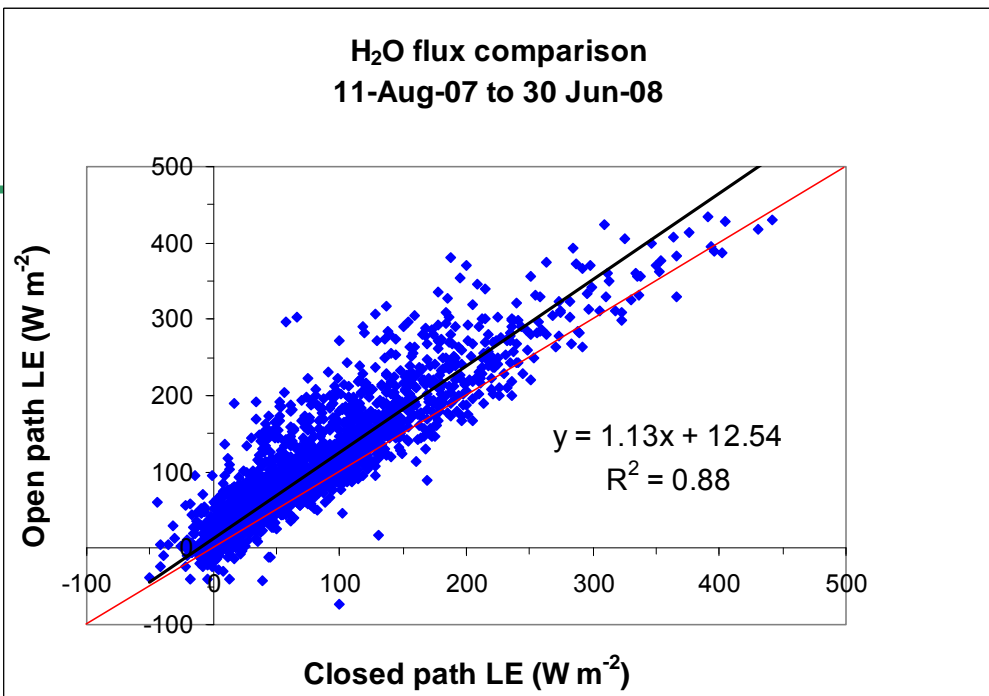


Time series of F_c

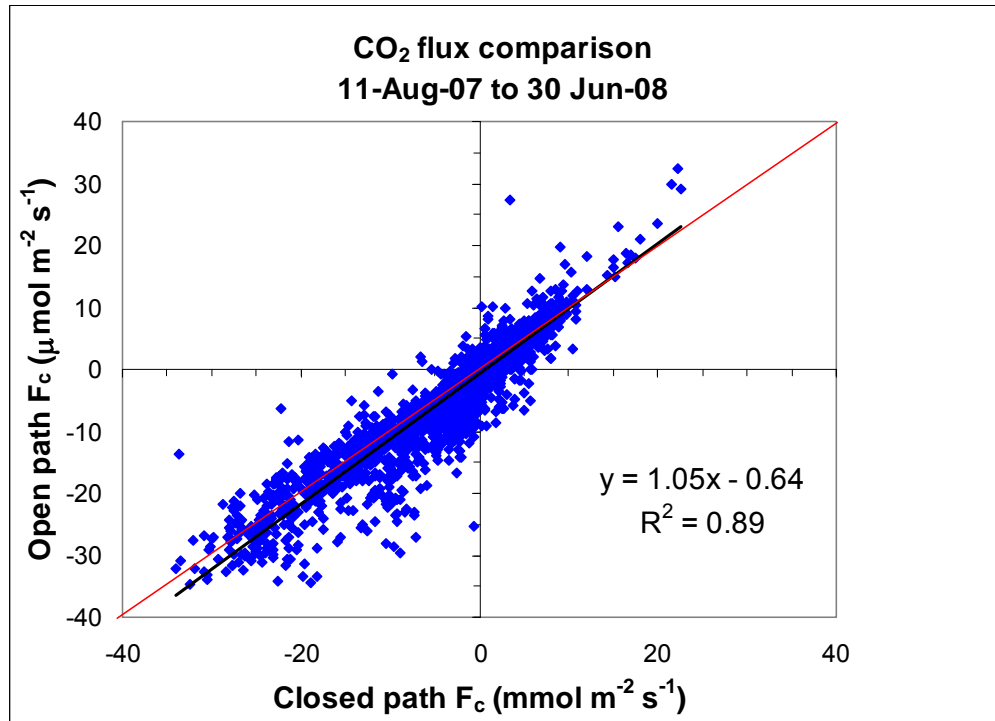


Open vs closed path instruments

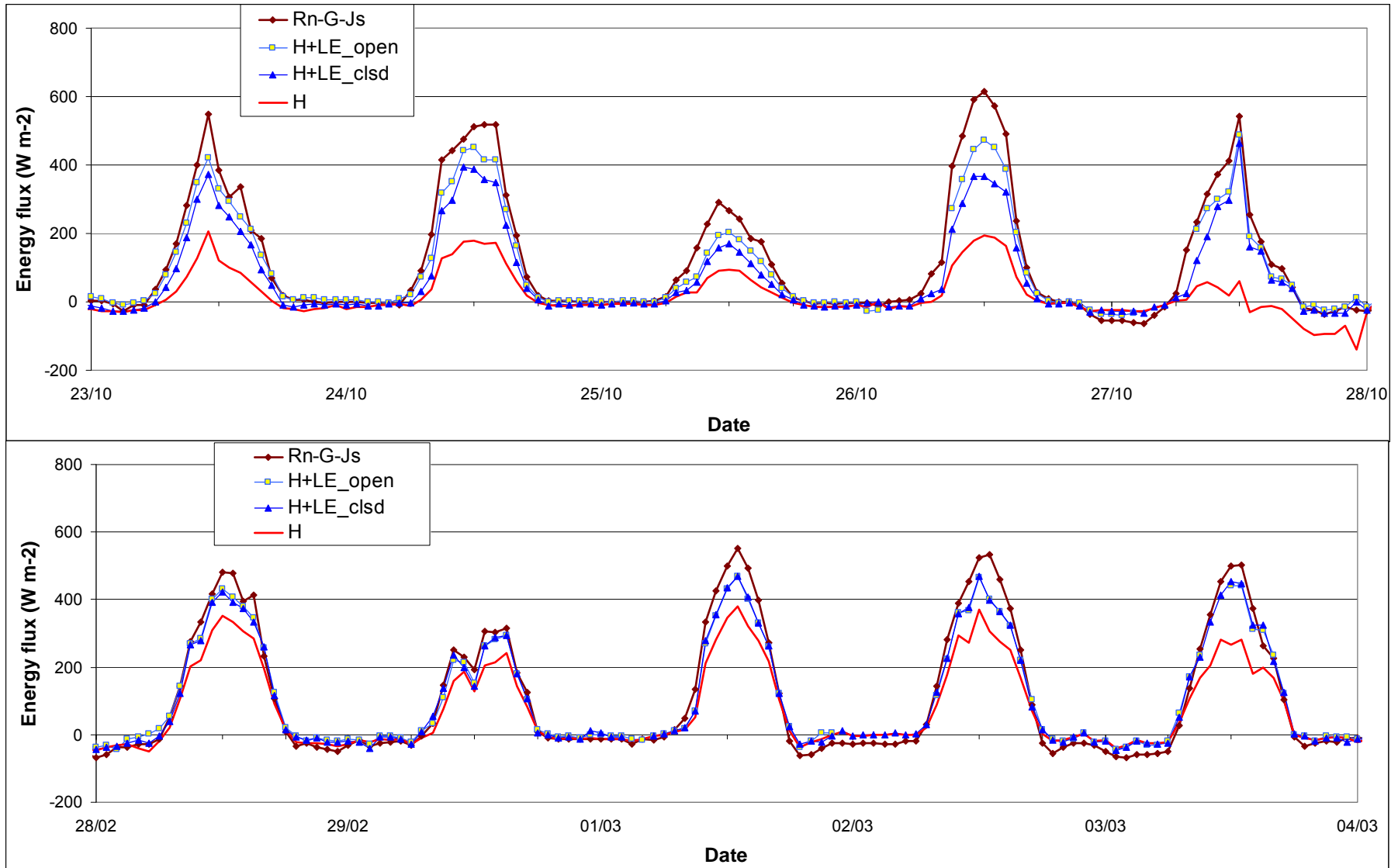
H₂O



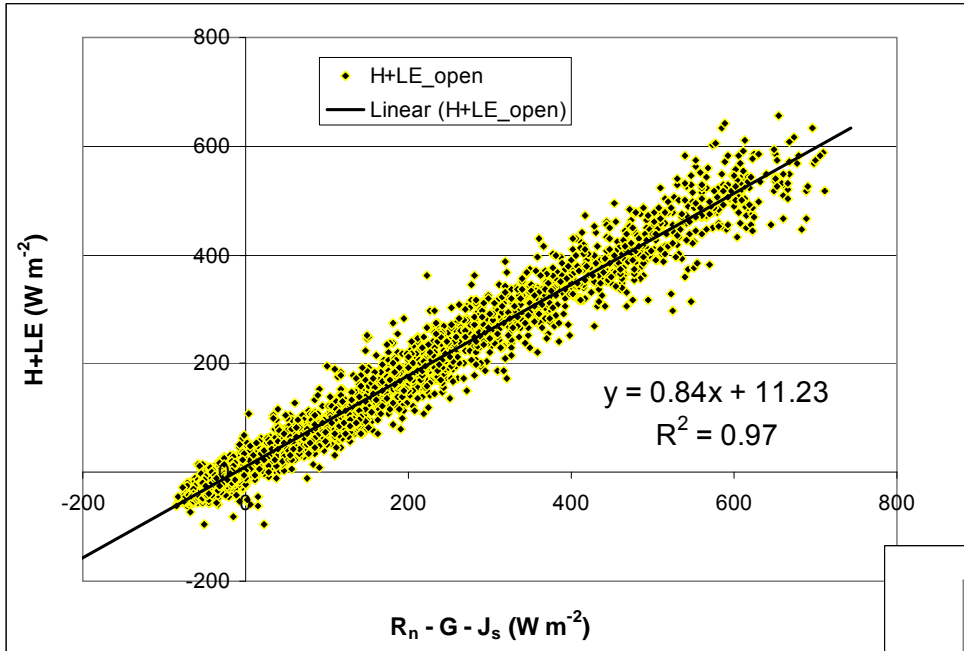
CO₂



Time series of $R_n - G - J_s$, $H + LE$ & H



Energy balance

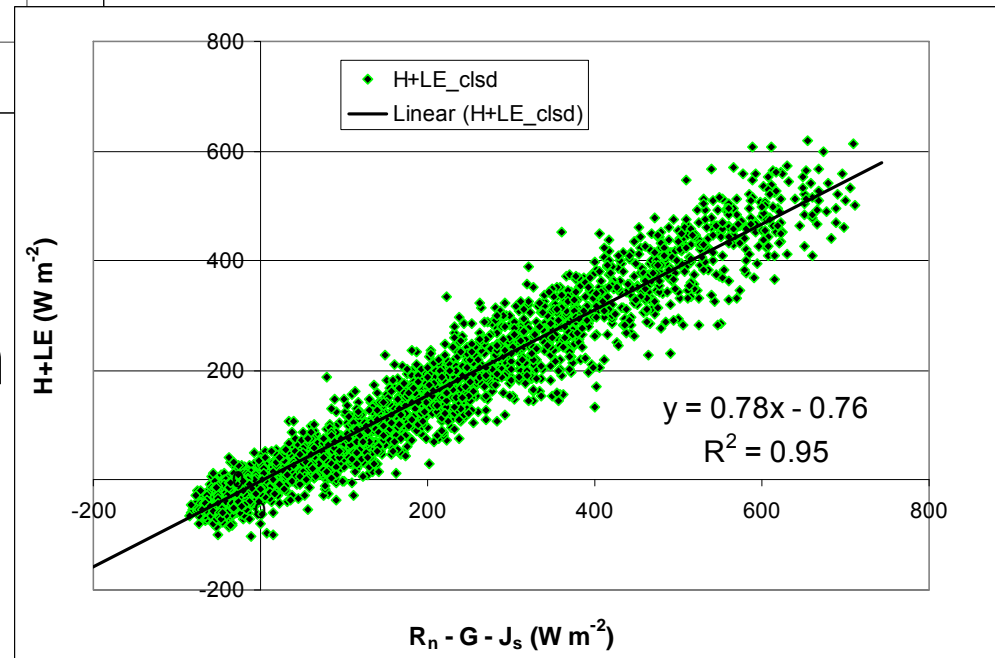


Open Path

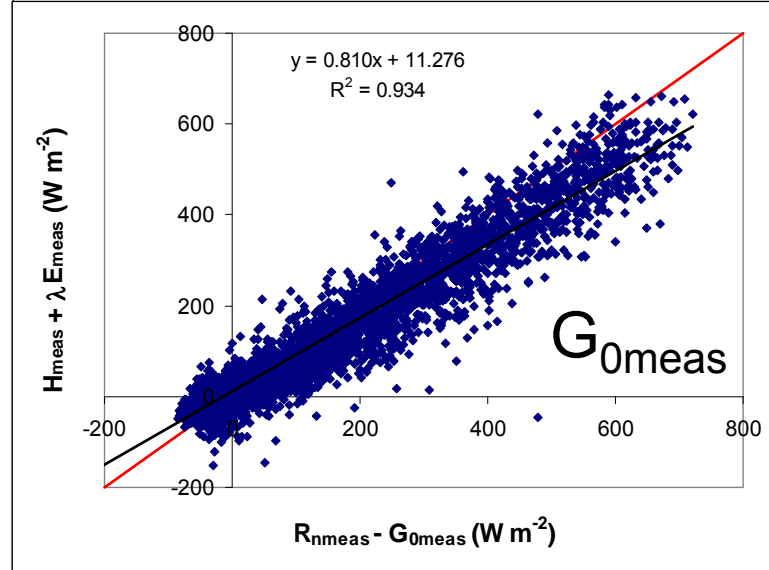
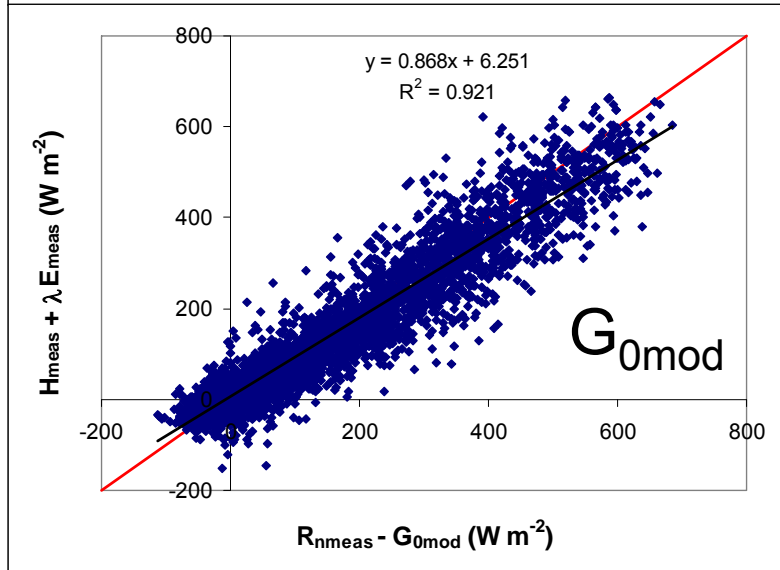
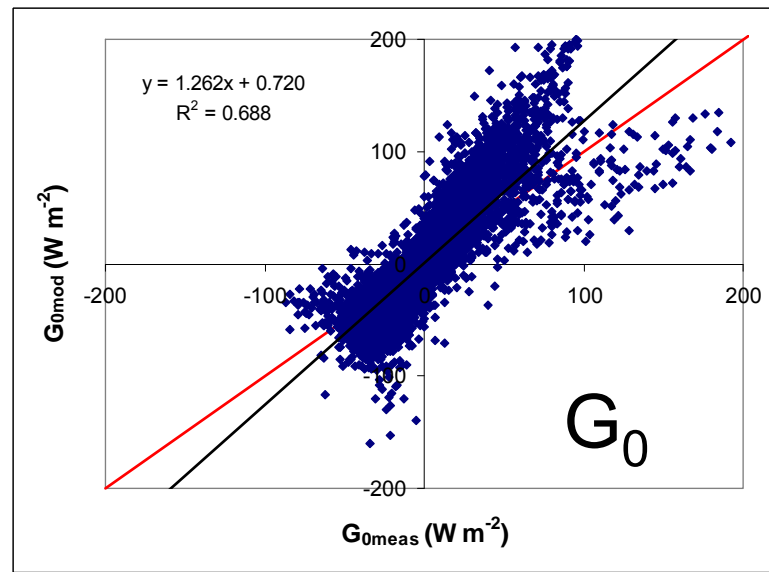
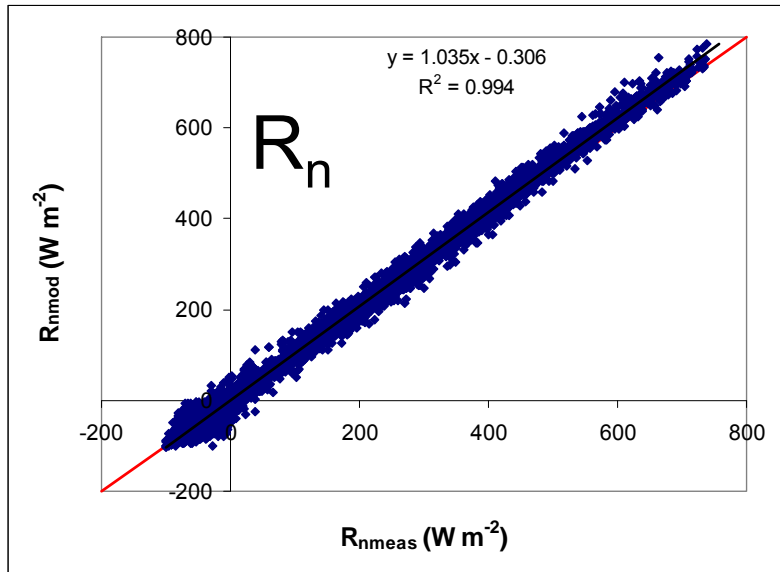
sma slope 0.850
lower b 0.845
upper b 0.854

Closed Path

sma slope 0.801
lower b 0.795
upper b 0.807



Modelling with CABLE



Summary (1):

- Open path analyser

- Strengths

- Excellent spectral & cospectral response compared to temperature
- Little need for high frequency correction due to line-averaging and instrument separation when measurements made at 4.5 m

- Weakness

- High rates of data loss at Otway – mist, rain ...
- WPL corrections to CO₂ fluxes very large when H is large

Summary (2):

- Closed path analyser
- Low rate of data loss due to rain, mist ...
- Calculate mixing ratios in real time – no WPL correction needed
- Strengths:CO₂
 - Good spectral & cospectral response compared to temperature
 - Well-defined lag as a function of flow rate
 - Close agreement with open path instrument

Strengths:H₂O

Agreement with open path instrument can be obtained with correction for loss of covariance at high frequencies

- Weakness
 - Poor spectral & cospectral response compared to temperature
 - Variable lag time @ maximum correlation – depends on flow rate and rel. humidity

Summary (3):

- Lack of energy closure
 - Better closure for open than closed path instruments
 - Change in energy storage term on layer above soil heat flux plates is very important but does not explain lack of energy closure
- Advection?
 - Horizontal temperature gradients \rightarrow advection $< 5 \text{ W m}^{-2}$
 - Vertical advection – needs non-zero mass flux of dry air